

# 1/16/2018 LECTURE NOTES

## SUBTRACTION

$$\vec{r}_1 = x_1 \hat{i} + y_1 \hat{j} + z_1 \hat{k}$$

$$\vec{r}_2 = x_2 \hat{i} + y_2 \hat{j} + z_2 \hat{k}$$

$$\vec{r}_2 - \vec{r}_1 = (x_2 - x_1) \hat{i} + (y_2 - y_1) \hat{j} + (z_2 - z_1) \hat{k}$$

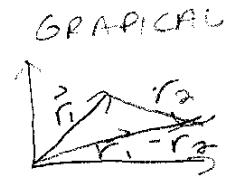
EXAMPLE - SUBTRACT  $\vec{r}_2 - \vec{r}_1$

$$\vec{r}_1 = 22.5 \text{ km } \hat{i} + 39.0 \text{ km } \hat{j}$$

$$\vec{r}_2 = 0.0797 \text{ km } \hat{i} + 0.0797 \text{ km } \hat{j} + 0.041 \text{ km } \hat{k}$$

$$\vec{r}_2 - \vec{r}_1 = (0.0797 - 22.5) \text{ km } \hat{i} + (0.0797 - 39.0) \text{ km } \hat{j} + (0.041 - 0) \text{ km } \hat{k}$$

$$= \boxed{-22.4 \text{ km } \hat{i} - 38.9 \text{ km } \hat{j} + 0.041 \text{ km } \hat{k}}$$



TURN THE PROTRACTOR UPSIDE DOWN FOR THE SECOND VECTOR

## MULTIPLICATION

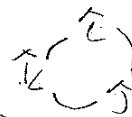
LAW OF COSINES

$$\vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \theta$$

LAW OF SINES

$$\vec{A} \times \vec{B} = |\vec{A}| |\vec{B}| \sin \theta$$

CROSS PRODUCT CIRCLE



CROSS TERMS STAY

CROSS TERMS CANCEL

OR

$$\vec{A} \cdot \vec{B} = \vec{r}_1 \cdot \vec{r}_2 = (x_1 x_2) + (y_1 y_2) + (z_1 z_2)$$

CROSS

$$\vec{A} \times \vec{B} = (y_1 z_2 - z_1 y_2) \hat{i} + (z_1 x_2 - x_1 z_2) \hat{j} + (x_1 y_2 - y_1 x_2) \hat{k}$$

## EXAMPLE

FIND THE DOT AND CROSS PRODUCT

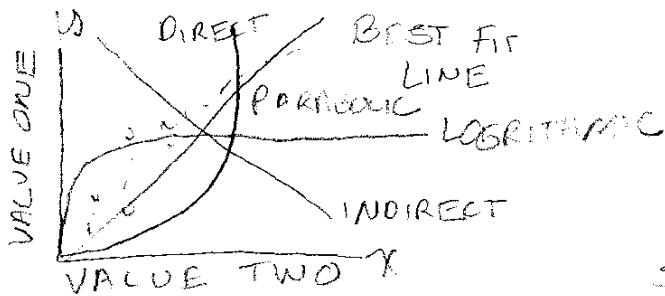
$$\vec{r}_1 = 22.5 \text{ km } \hat{i} + 39.0 \text{ km } \hat{j}$$

$$\vec{r}_2 = 0.0797 \text{ km } \hat{i} + 0.0797 \text{ km } \hat{j} + 0.041 \hat{k}$$

$$\begin{aligned} \vec{r}_1 \cdot \vec{r}_2 &= (22.5 + 0.0797) \text{ km}^2 + (39.0 \cdot 0.0797) \text{ km}^2 + (0)(0.041) \text{ km}^2 \\ &= \boxed{4.90 \text{ km}^2} \end{aligned}$$

$$\begin{aligned} \vec{r}_1 \times \vec{r}_2 &= (39.0(0.041) - (0)(0.0797)) \text{ km}^2 \hat{i} + ((0)(0.0797) - (22.5)(0.041)) \\ &\quad \text{km}^2 \hat{j} + ((22.5)(0.0797) - (39.0)(0.0797)) \text{ km}^2 \hat{k} \\ &= \boxed{1.59 \text{ km}^2 \hat{i} - 0.92 \text{ km}^2 \hat{j} - 1.32 \text{ km}^2 \hat{k}} \end{aligned}$$

TO FIND THE MAGNITUDE ALONG A CERTAIN AXIS WE NEED TO FIND THE RELATIONSHIP. SOMETIMES WE USE  $y = mx + b$  (SLOPE-INTERCEPT)



NEED TO FIND  
AVERAGE SLOPE  
AND AVERAGE INTERCEPT

$$\text{SLOPE} = m = \frac{\text{RISE}}{\text{RUN}} = \frac{y_2 - y_1}{x_2 - x_1}$$

EXAMPLE (THIS MAY NOT BE THE SAME AS IN CLASS)

FIND THE SLOPE INTERCEPT

x	y
0	2) m <sub>1</sub>
2	5) m <sub>2</sub>
4	9) m <sub>3</sub>
6	13) m <sub>4</sub>
10	18) m <sub>5</sub>
12	23) m <sub>5</sub>

$$m_1 = \frac{5-2}{2-0} = 1.5$$

$$m_2 = \frac{9-5}{4-2} = 2$$

$$m_3 = \frac{13-9}{6-4} = 2$$

$$m_4 = \frac{18-13}{10-6} = 1.25$$

$$m_5 = \frac{23-18}{12-10} = 2.5$$

$$m_{\text{AVE}} = 1.85$$

$$y = mx + b \quad \text{SOLVE FOR } b$$

$$-mx \quad -mx$$

$$y - mx = b \quad m = 1.85$$

$$b_1 = 2 - (1.85)(0) = 2$$

$$b_2 = 5 - (1.85)(2) = 1.3$$

$$b_3 = 9 - (1.85)(4) = 1.6$$

$$b_4 = 13 - (1.85)(6) = 1.9$$

$$b_5 = 18 - (1.85)(8) = 2.2$$

$$b_6 = 23 - (1.85)(10) = 2.5$$

$$b_{AVE} = 1.18$$

$$y = 1.85x + 1.18$$